

Image processing



About

- Broad field that includes low-level operations as well as complex high-level algorithms
 - Low-level image processing
 - Computer vision
 - Computational photography
- Several procedures and concepts of that are frequently used in the context of multimedia systems
- Can also be applies to videos (frame by frame)



Image as a matrix

- 2D array (width x height)
- Channels
 - RGB = 3 channels
 - Sampling resolution

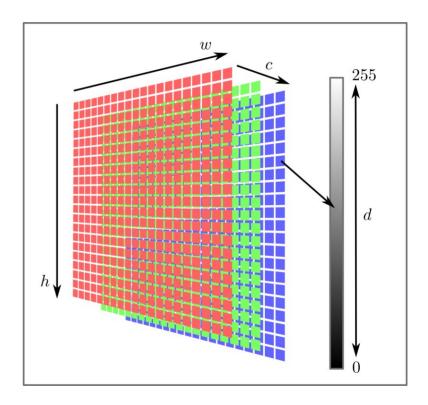




Image as a function

- Image is a 2D function: $f: \mathcal{R}^2 \to \mathcal{R}$
 - Defined over a rectangle $\ [0,H] \times [0,W]$
 - Has a finite range [0,1]
 - Color image is defined as a triplet of functions

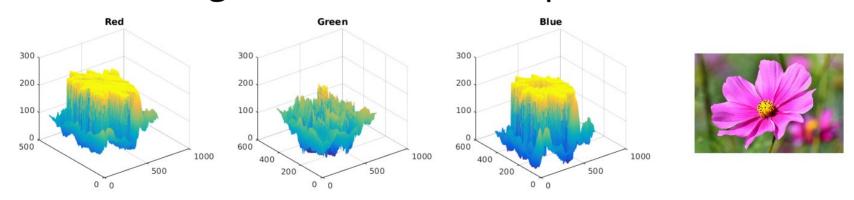




Image operations

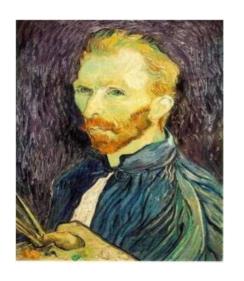
- Intensity transformations
 - Pixel-wise
 - Histogram
 - Filtering
- Geometrical transformations
 - Linear
 - Local
- Complex operations
 - Context-aware resizing
 - Compositing
 - Segmentation

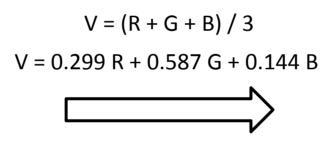




Conversion to grayscale

From RGB: (weighted) averaging of channels



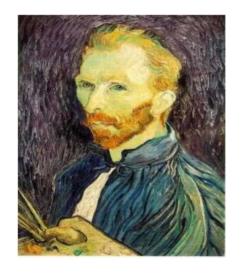


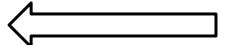




Conversion from grayscale

How is gray represented in RGB color space?









Pixel-wise operation: negation

8-bit intensities are defined on interval from 0 to 255

Image negation of image A is B = (255 - A)

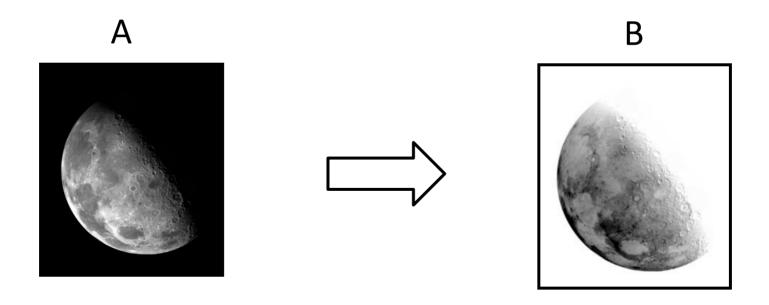
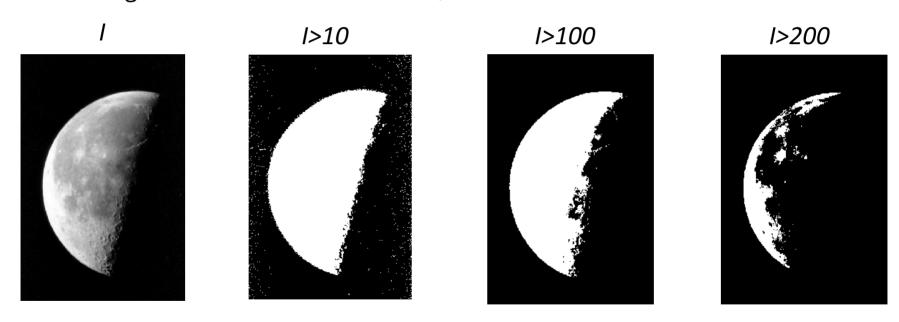




Image threshold

Pixel values higher than value T are set to 1, others to 0



Object segmentation: determining a suitable threshold is not trivial



Brightness and contrast

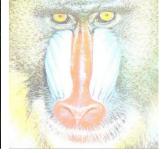
- Brightness intensity of a pixel relative to another pixel
- Contrast difference between minimum and maximum pixel

$$f(x) = \alpha x + \beta$$

$$f(x) = \alpha(x - 128) + 128 + b$$









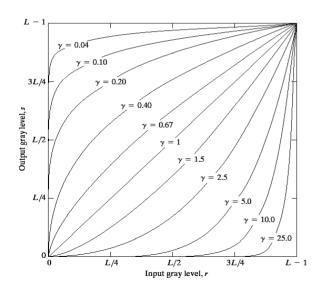


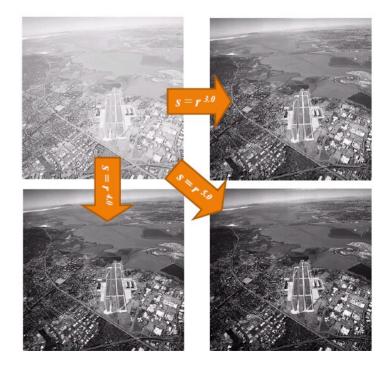




Nonlinear transformations

- Parametric function that maps source values **r** to destination values **s**.
- Exponential function family $s=cr^{\gamma}$
- Parameter c is usually 1
- Parameter r is in [0, 1]



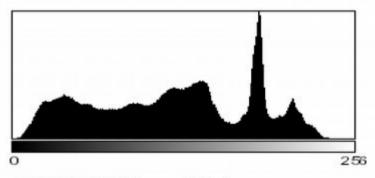




Distribution of values in images

- How to adjust values based on the image?
- Use image-specific statistics histograms





Count: 1920000 Mean: 118.848

StdDev: 59.179

Min: 0 Max: 251

Mode: 184 (30513)

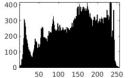


Histogram

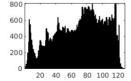
- Frequency of different pixel values
 - How often they occur in image
 - Sub-sampling into cells/buckets
- Robust description
 - Rotation
 - **Translation**
 - Scale



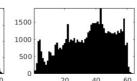




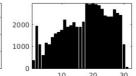






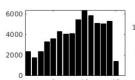


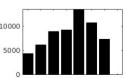


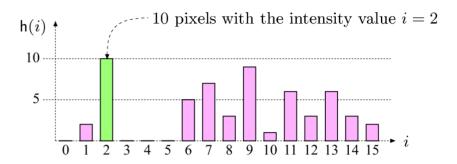


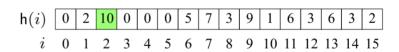














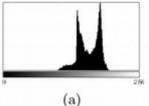
Histogram and image quality

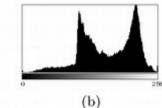
- Increase/reduce brightness:
 - Histogram shifts left/right
- Increase/reduce contrast:
 - Histogram is shrinking/stretching

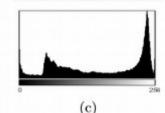








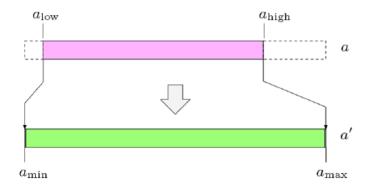




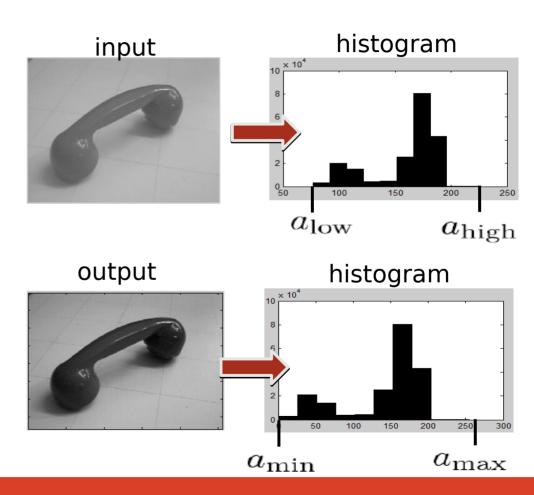


Histogram stretching

$$f_{\rm ac}(a) = a_{\rm min} + (a - a_{\rm low}) \cdot \frac{a_{\rm max} - a_{\rm min}}{a_{\rm high} - a_{\rm low}}$$



Operation performed on each pixel individually.



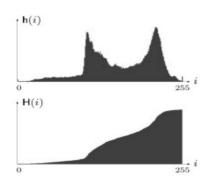


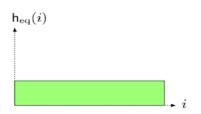
Histogram equalization

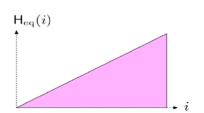
- Cumulative histogram value dynamics
- $H(i) = \begin{cases} h(0) & \text{for } i = 0 \\ H(i-1) + h(i) & \text{for } 0 < i < K \end{cases}$

- Desired dynamics is uniform
- Transform image values so that the cumulative histogram is diagonal.





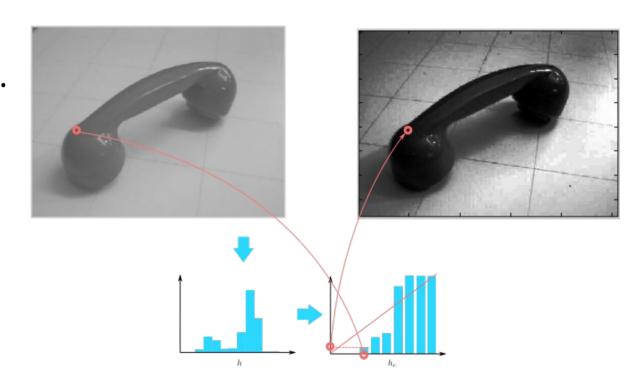






Equalization algorithm

- Compute 256-bin histogram of image I (h).
- Compute cumulative histogram (hc).
- Normalize (hc) with maximum value, multiply by 255 (hnc)
- Use (hnc) as a lookup table to transform individual pixels.





Histogram equalization in color images



Original







RGB Equalized Independently

Because each channel is transformed independently, the resulting color changes as well.



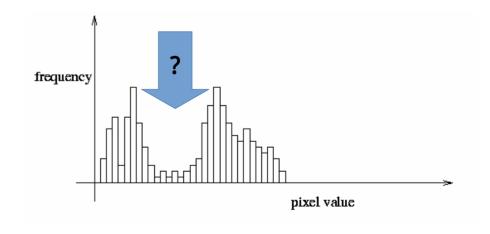
Luminance Equalization

Transform to color space with separate luminance channel, equalize only intensity



Histogram and thresholding

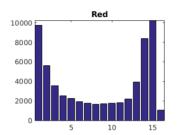
- Analyze histogram to find good threshold
- Bi-modal histogram
- Otsu method
 - Minimize variance of foreground and background

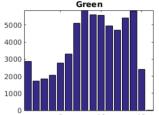


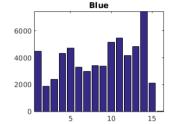


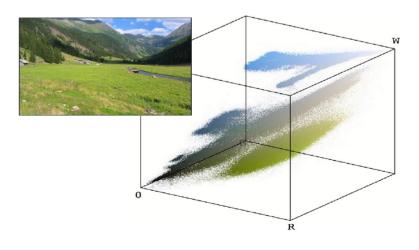
Color histogram

- 3 histograms
 - Each component separate
 - No correlation
 - Less space
- 3D histogram
 - Image color is a 3D index
 - More specific
 - More space





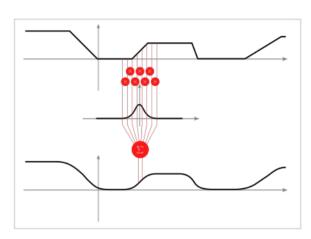


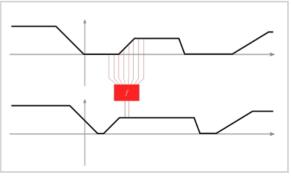


Filtering

Vicos sualgnitive ystemslab

- Resulting value dependent on the neighborhood
- Linear filters
 - Convolution / correlation
 - Kernel function (parameters)
 - Associativity, separability
- Nonlinear filters
 - Arbitrary (local) operation
 - Max, min
 - Median





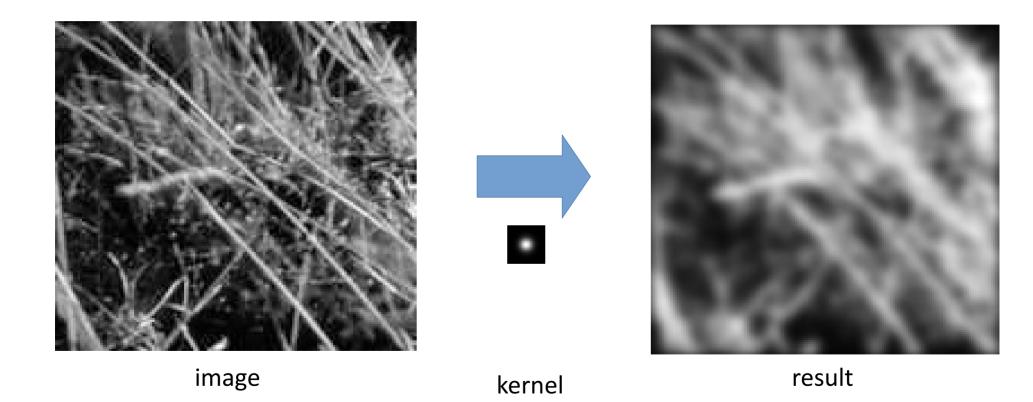


Simple, yet complex

- Single linear filter
 - Blur, directional blur
 - Edges, blobs
- Multiple linear filters that are learned
 - Extract specific properties
 - Data-driven
 - Convolutional neural networks



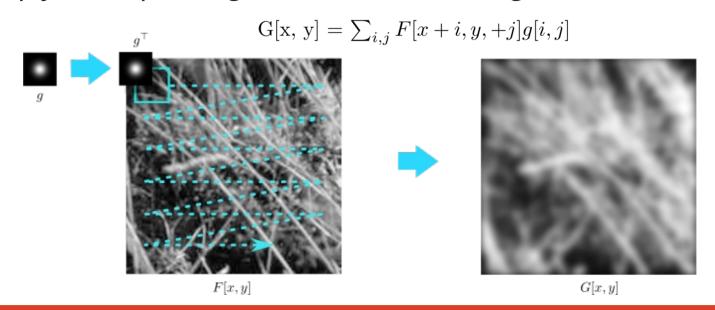
Linear filters



Vices sualgnitive ystemslab

In a nutshell

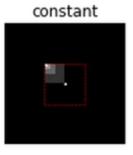
- How to compute filter response in individual pixel?
 - Transpose kernel (convolution) and align its center with the pixel
 - Multiply corresponding elements and sum together

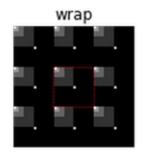


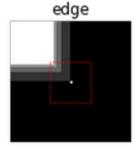
What to do with borders?

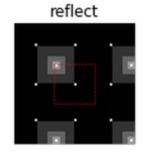
Vicos sualgnitive ystemslab

- Image is a finite signal
 - Filtering
 - Interpolation
- Data out of border has to be fabricated
- Different techniques
 - Based on use-case



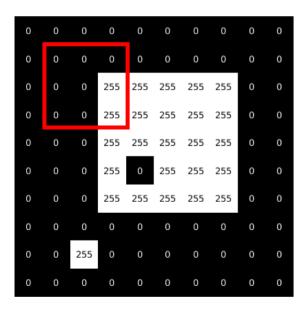




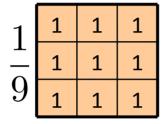




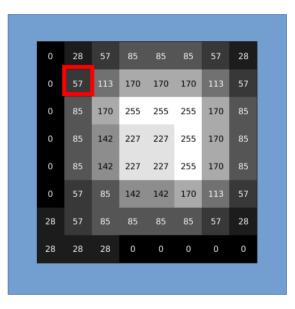
Weighted sum



g



G[x, y]

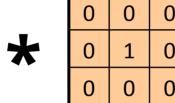


what do to with the border?

Identity filter





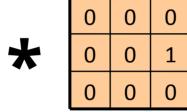


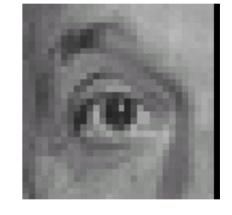


Shift filter



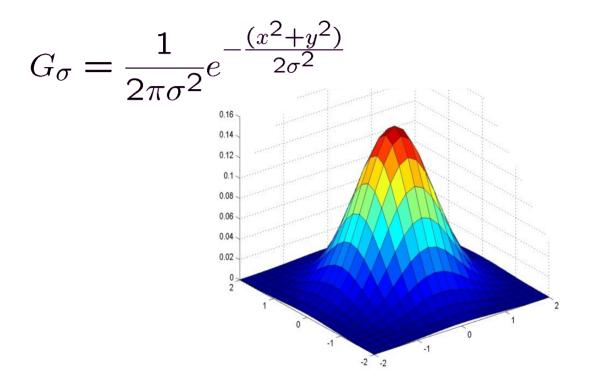


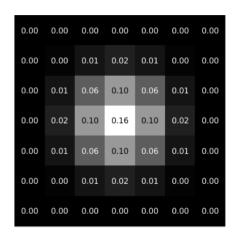




Vicos sualgnitive ystemslab

Gaussian kernel





$$7 \times 7$$
, sum = 1

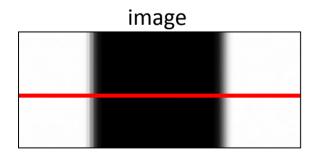
Constant before the exponential function ensures that the sum of the elements is always 1 (in continuous space).

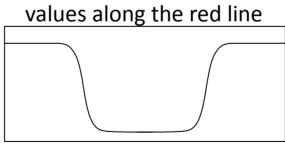


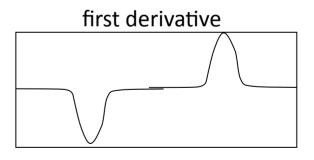
Detecting edges

- Goal: find sudden changes in illumination in the image
- Ideal: line drawing by an artist (semantic knowledge)









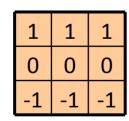


Using convolution

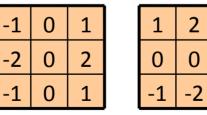
- Kernel can represent approximation of image derivation
- We use separate kernels for vertical and horizontal derivation

Prewitt

-1	0	1
-1	0	1
-1	0	1



Sobel



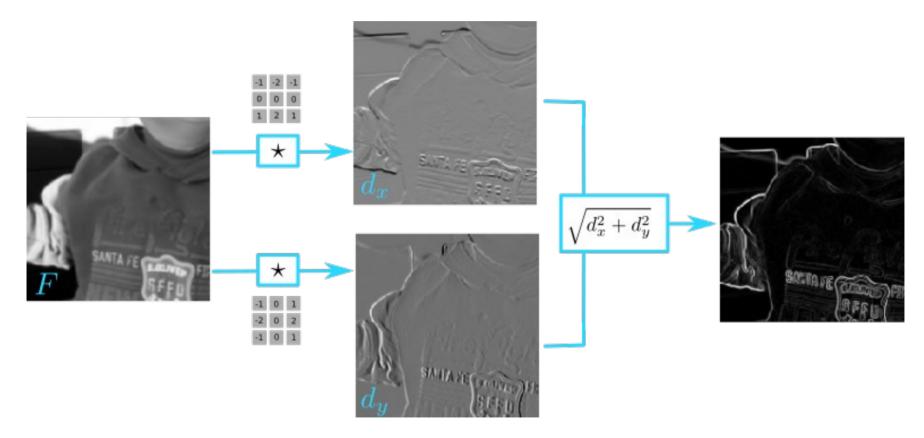
Roberts

0	1
-1	0



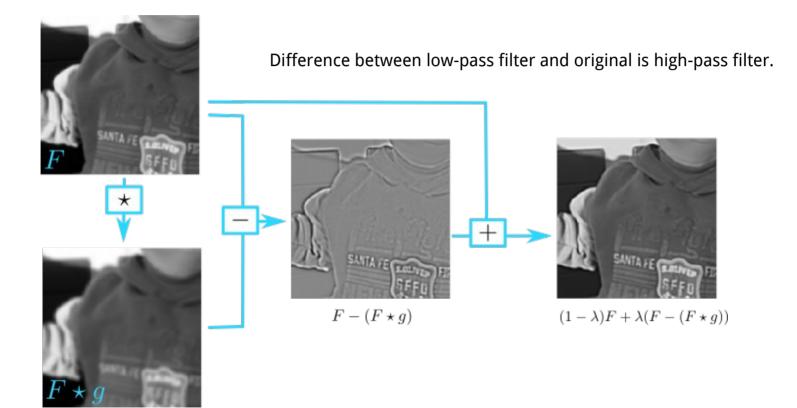


Derivative magnitude





Sharpening by blurring



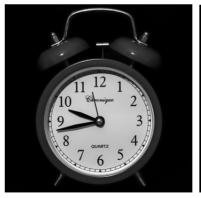
Non-linear filters

Vicos sualgnitive ystemslab

- Median: middle element by value
- Bilateral filter
 - Weights based on neighborhood
 - Preserves edges
- Morphological operations
 - Max: highest element in neighborhood
 - Min: lowest element in neighborhood



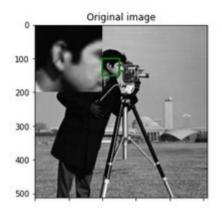


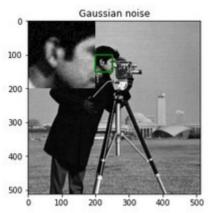




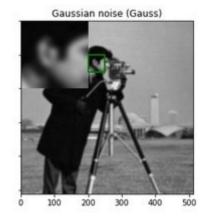


Gaussian noise removal

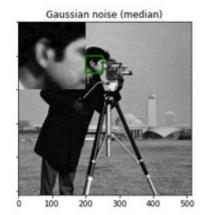




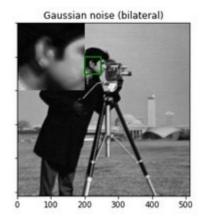






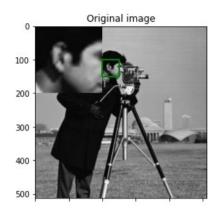








Salt&pepper noise removal



Salt&pepper noise

100

200

400

500

100

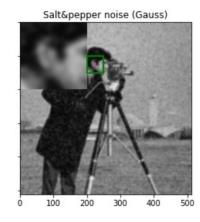
200

300

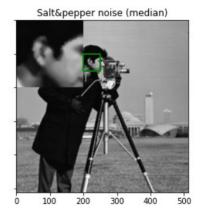
400

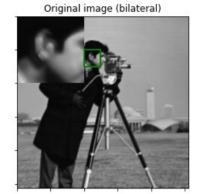
500

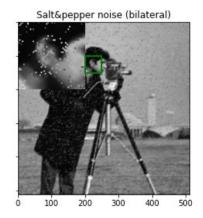








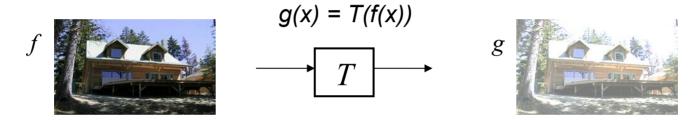




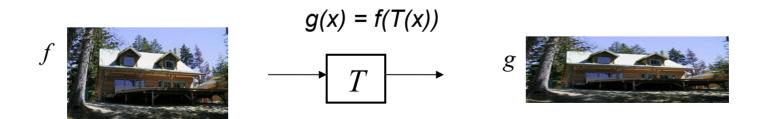


Geometry vs. intensity

Image filtering is foremost an intensity transformation

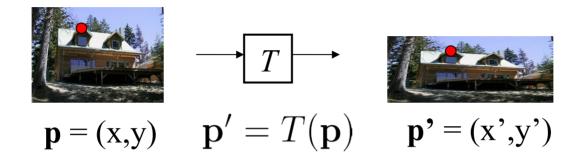


Geometry transformation changes geometry of the image





Parametric transformations



- Transformation T changes coordinates of pixel p
- Global transformation changes all pixels in the same way

$$\left[\begin{array}{c} x' \\ y' \end{array}\right] = \mathbf{M} \left[\begin{array}{c} x \\ y \end{array}\right] \qquad \mathbf{p}' = \mathbf{M} \cdot \mathbf{p}$$



I inear transformations

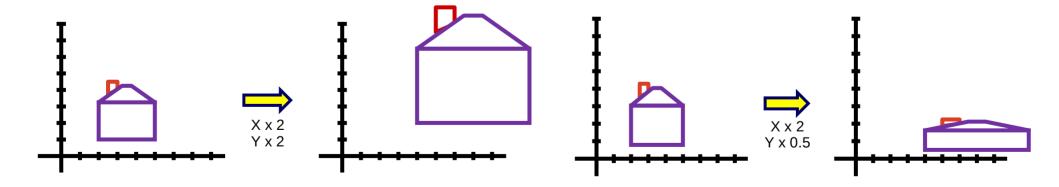
Rotation:

• Shear:



Scaling

- Multiply coordinates with a scalar
 - Uniform same scalar for all axes
 - Non-uniform different scalar





Translation

Translation is not homogeneous in 2D space

$$x' = x + t_x$$
$$y' = y + t_y$$

$$\mathbf{M} = \left[egin{array}{ccc} 1 & 0 & t_x \ 0 & 1 & t_y \ 0 & 0 & 1 \end{array}
ight] \qquad \left[egin{array}{c} x' \ y' \end{array}
ight] = \mathbf{M} \, \left[egin{array}{c} x \ y \end{array}
ight]$$

• We can use homogeneous coordinates
$$\begin{bmatrix} x \\ y \end{bmatrix} \Longrightarrow \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



Homogeneous coordinates

2D space: transformation matrix of size 3x3

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & \alpha_x & 0 \\ \alpha_y & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

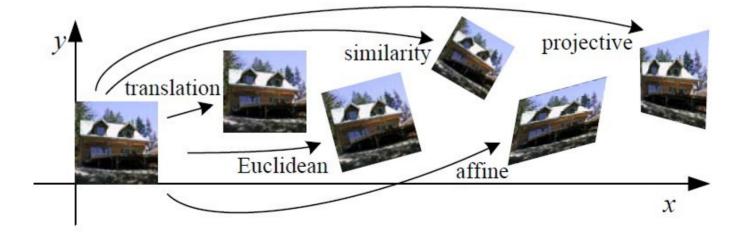
General projective transform

$$\left[\begin{array}{c} x'\\y'\\1\end{array}\right] = \lambda \left[\begin{array}{ccc} a & b & c\\d & e & f\\g & h & i\end{array}\right] \left[\begin{array}{c} x\\y\\1\end{array}\right]$$



Common transformations

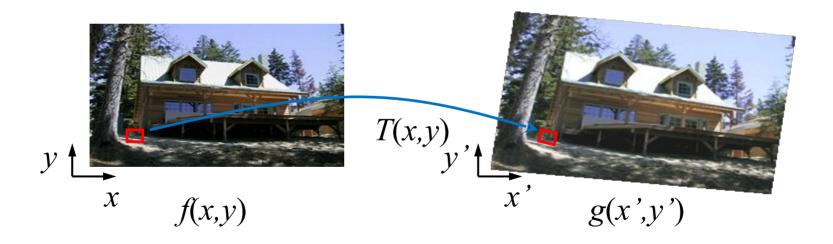
- Translation
- Euclidean transform (translation, rotation)
- Similarity transform (translation, rotation, scaling)
- Affine transform (maintains parallelism of straight lines)
- Projective transform





Warping

Given transform [x',y'] = T(x,y) and f(x,y), how to compute g(x',y') = f(T(x,y))?



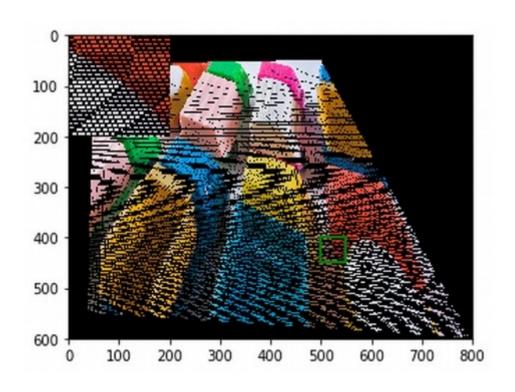


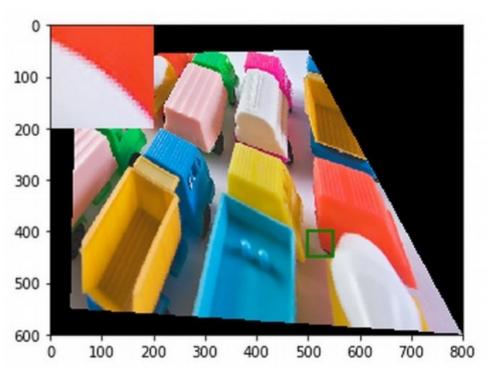
Naive approach

- For each pixel f with coordinates (x,y)
 - Compute transformed coordinates [x',y']=T(x,y).
 - Copy color of f(x,y) to new image at coordinates g(x',y')
- Why is it naive?
 - We visit all pixels in f(x,y)
 - Do we visit all pixels of g(x,y)?



Example

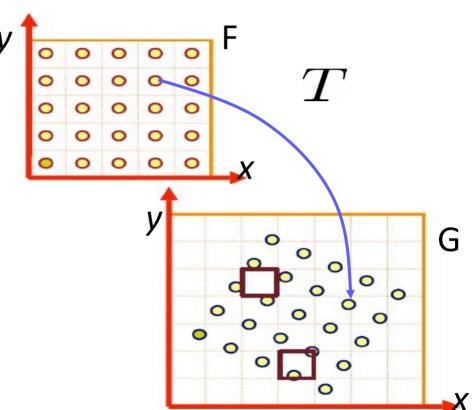






Asymmetry of discretization

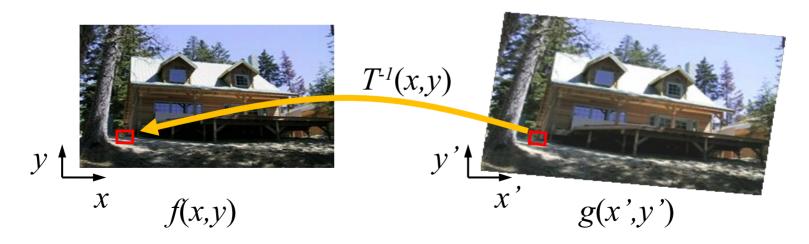
- A single pixel of F is mapped to more pixels in G.
- Pixel in F is not mapped to any pixel in G.
- Visit all pixels in G





Inverse mapping approach

- For each pixel in g with coordinates (x',y')
 - Compute old coordinates using inverse transform [x,y]=T-1(x',y')
 - We copy pixel color of f(x,y) to g(x',y')
- We visit all pixels in g
- Pixel from g can transform to more than one pixel in f





Resizing the image

- Adjusting (local or global) resolution in image.
- Two general cases:
 - Reduction / decimation / down-sampling shrinking image
 - Interpolation / up-sampling enlarging image







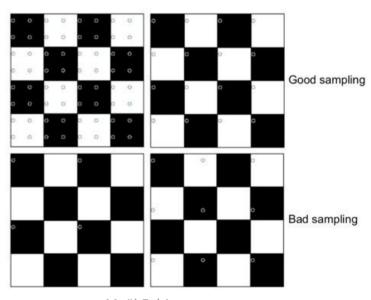






Decimation approaches

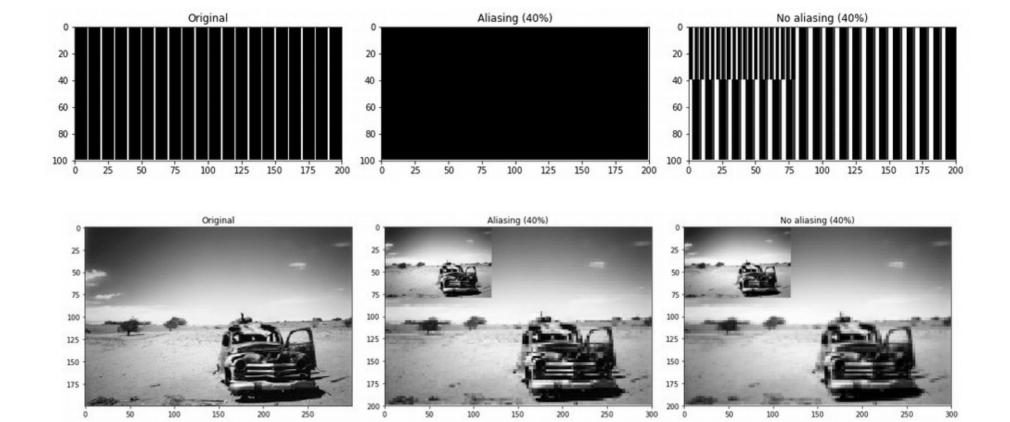
- Sampling values
 - ullet Shannon sampling theorem $f_s \geq 2 f_{max}$
 - Remove high frequencies
- Anti-aliasing
 - First remove high frequencies
 - Then subsample with appropriate frequency
- Filters used
 - Gaussian
 - Lanczos kernel



Maël Fabien



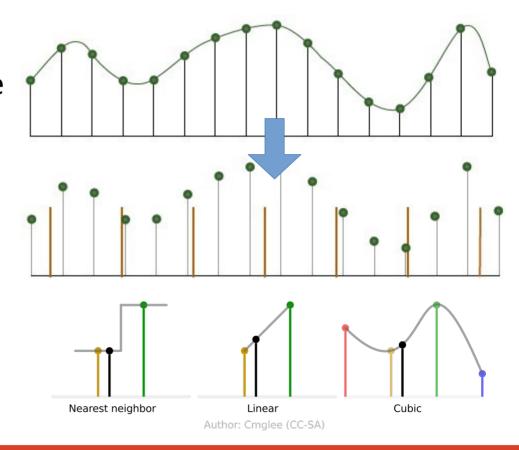
Decimation examples





Up-sampling – guessing the values

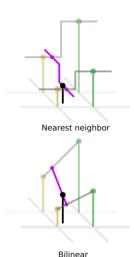
- Nearest neighbor
 - Take value of the closest sample
- Linear interpolation
 - Use two values
 - Fit linear function
- Cubic interpolation
 - Use four values
 - Fit third-degree polynomial

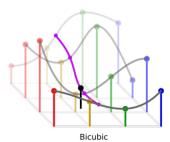


Interpolation in images

Vicos sualgnitive ystemslab

- Nearest neighbour
 - Take pixel closest to desired coordinates
- Bilinear
 - Use four closest pixels
 - Estimating a plane
- Bicubic
 - Use 16 closest pixels
 - Estimating a polynomial surface
 - Slower

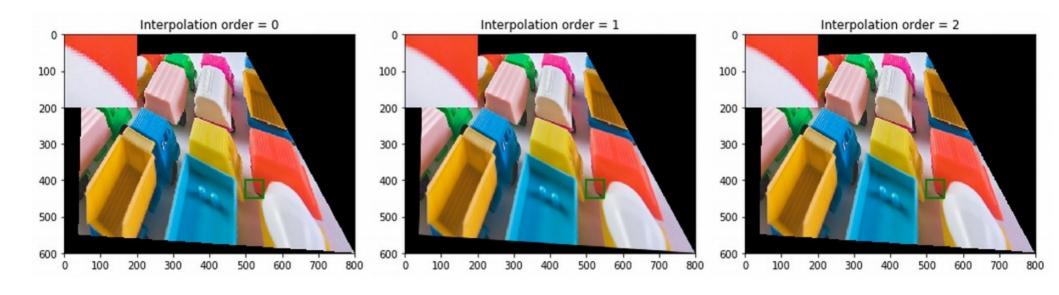




Author: Cmglee (CC-SA)



Interpolation examples





Non-linear transformations

- Camera rectification
 - Counter lens distortions
 - Camera calibration model
- Locally-linear transformation
 - Local regions are transformed locally
 - Image morphing







Image morphing



How to deform image A to image B?

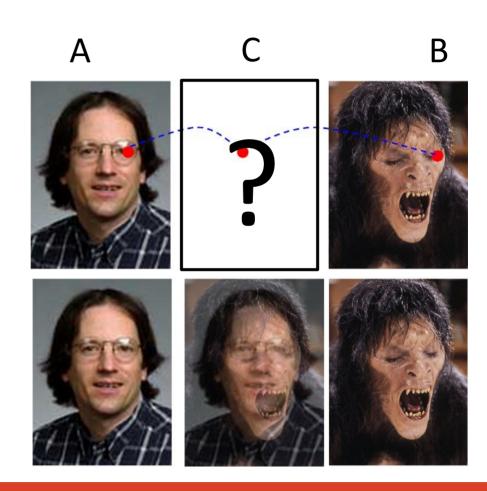


Image morphing

- How to compute intermediate image C
- Naive approach weighted sum of pixels

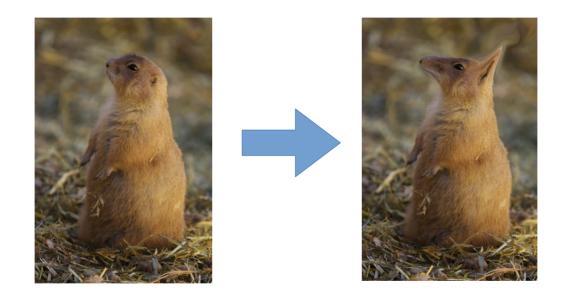
$$C_t = \alpha_t A + (1 - \alpha_t) B$$
$$0 \le \alpha_t \le 1$$

 Not realistic - not combining semantic parts





Dense deformation field



Mapping each pixel into its new location

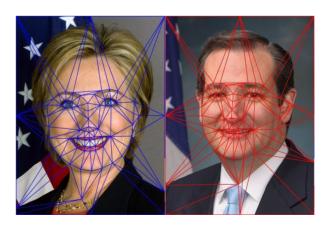


Deformation field approximation

- Determining entire field is time-consuming
- Locally linear transformation
- Correspondences control points
- Delaunay triangulation, interpolation









Control points

Control points mark matching pixels in both images

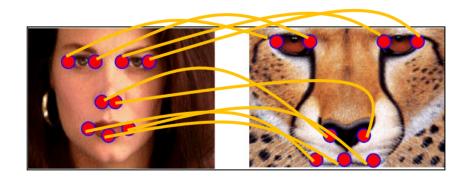






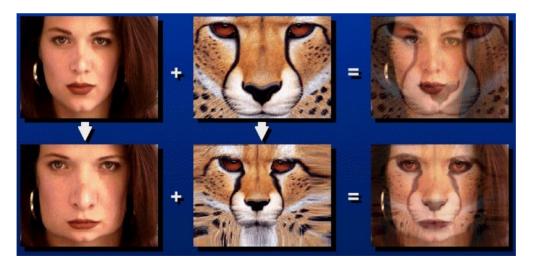


Image morphing overview

- For each image Ct compute ...
 - Interpolated position of control points
 - Two transformations: dA = A Ct and dB = B Ct
 - Blend colors of interpolated images

$$\mathbf{x}_i^C = \alpha_t \mathbf{x}_i^A + (1 - \alpha_t) \mathbf{x}_i^B$$

$$C_t = \alpha_t dA + (1 - \alpha_t) dB$$



Naive

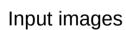
Correct



Morphing example









Control points





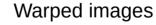








Blended image

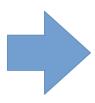






One more morphing example













Content-aware resizing

- Change size, aspect
- Automatically preserve important structures

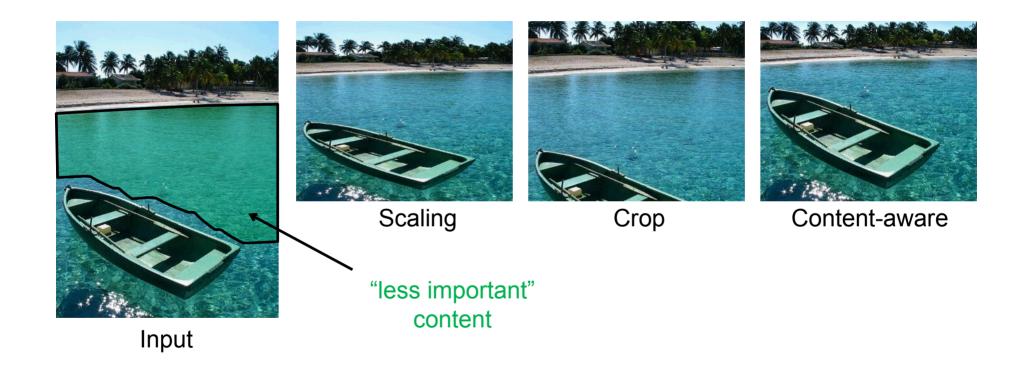








Important vs. unimportant content





Content-aware resizing

- General ideas
 - Adhere geometric constraints (size)
 - Preserve important structures
 - Reduce image artifacts
- Weakly conditioned problem
 - What is important? / Universal importance measure?
 - Would more people agree on the process?
 - Aesthetic rating (composition, ...)?



What is important in images?

What do people consider important?







Fast approximation - edges



How to remove?





Optimal (pixels with least energy)



Pixels with least energy in row



Columns with least energy



Seam carving

- We want to shrink image in one direction
- Basic idea: remove unimportant pixels
- Unimportant = little energy = little change = little edge
- Intuition
 - Preserve strong contours
 - Human perception is more sensitive to local changes
- Simple but achieves good performance



Image seam

 Connected path of pixels from the top to bottom







Determining optimal seam

- Optimal connected path of pixels from the top to the bottom that minimizes energy
 - Dynamic programming
 - Cummulative cost
 - Backtracking

5	8	12	3
9	2	3	9
7	3	4	2
4	5	7	8

$$M(i,j) = E(i,j) + \min(M(i-1,j-1), M(i-1,j), M(i-1,j+1))$$



Removing a seam

- Compute edge energy
- Compute cumulative energy
- Determine optimal seam
- Remove seam









Examples – reducing width









Examples – reducing height









Examples – scaling down







Interactive demo: https://www.aryan.app/seam-carving/



Image compositing

Combine images by taking pixels from appropriate images









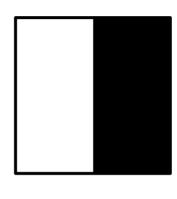




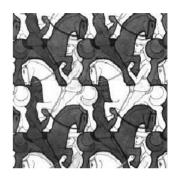
Naive combination – binary mask







R



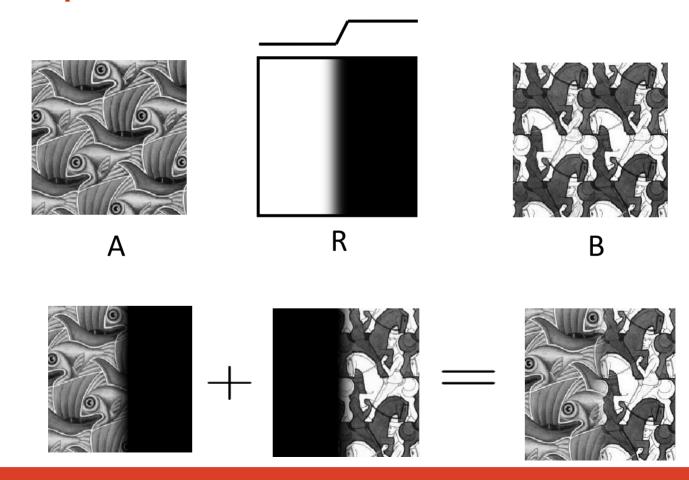
В

$$RA + (1 - R)B =$$





Smooth alpha channel





Example

Sharp transition – unreal image







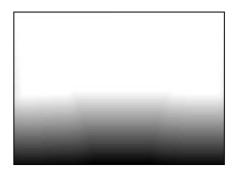




• Smooth transition – more realistic













Smoothing influence

Very smooth transition - ghosting











Sharp transition - cutoff

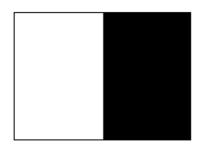


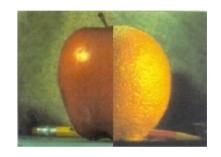
Frequency-aware blending

Simple alpha mask blending









 More natural effect if we blend images by frequency bands

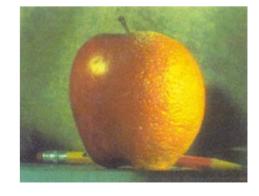
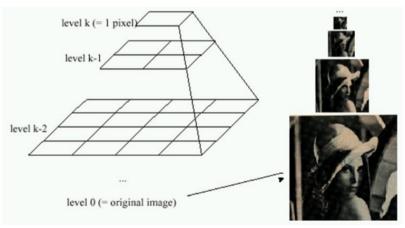




Image pyramids

- Multi-scale signal representation
 - Sequence of images
 - Each image only includes lower frequencies
- Gaussian pyramid
 - Smooth with Gaussian filter
 - Reduce resolution by half
 - Repeat







Gaussian pyramid

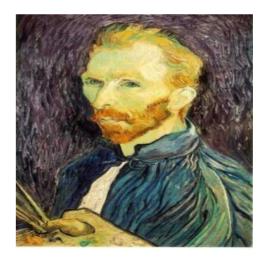
- Kernel size fixed
- Discard every second pixel
- Each layer removes frequency band



G 1/8



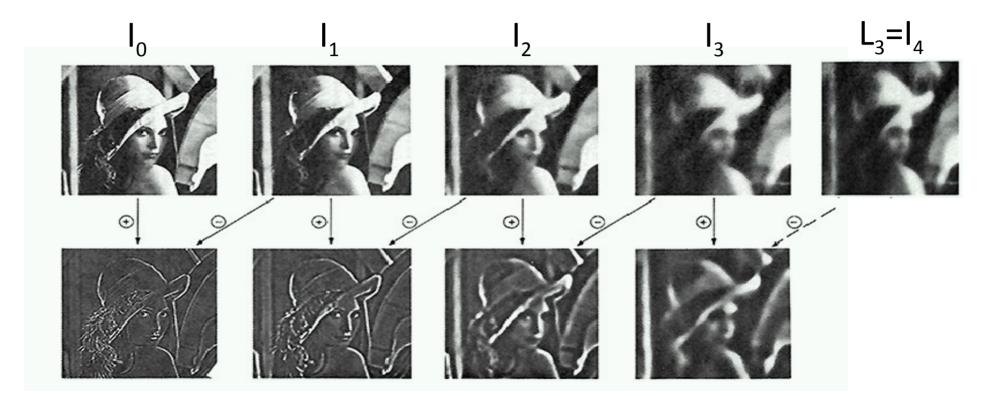
G 1/4



G 1/2



Laplacian pyramid



High frequencies

Medium frequencies

Low frequencies



Collapsing the pyramid



Reconstruction by collapsing pyramid

$$L_0 + L_1 + L_2 + L_3 = (I_0 - I_1) + (I_1 - I_2) + (I_2 - I_3) + I_3 = I_0$$

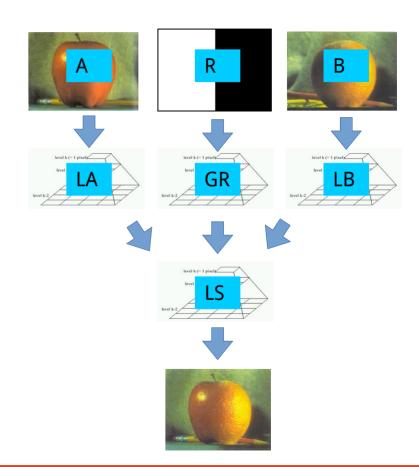


Laplacian blending algorithm

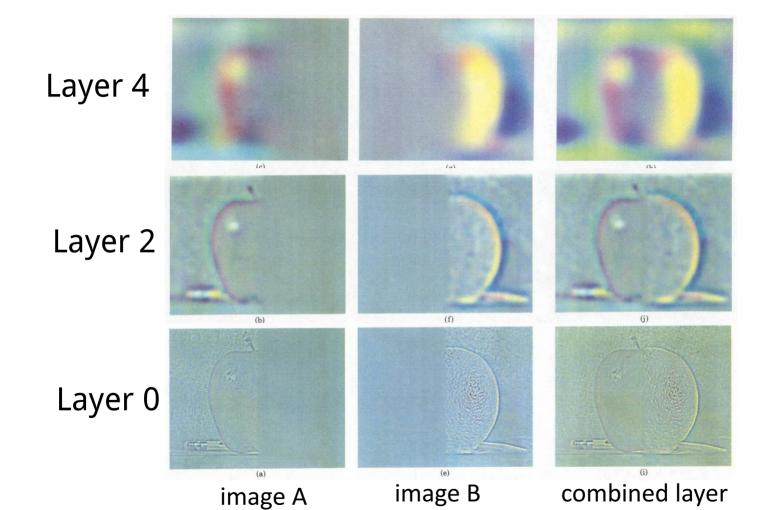
- Generate Laplacian pyramids LA and LB for images A and B
- Generate Gaussian pyramid GR for the alpha mask R
- Combine new Laplacian pyramid LS by combining corresponding layers from LA and LB using weights from the corresponding layer in GR:

$$LS_i = GR_i LA_i + (1 - GR_i) LB_i$$

Collapse pyramid LS into the resulting image S

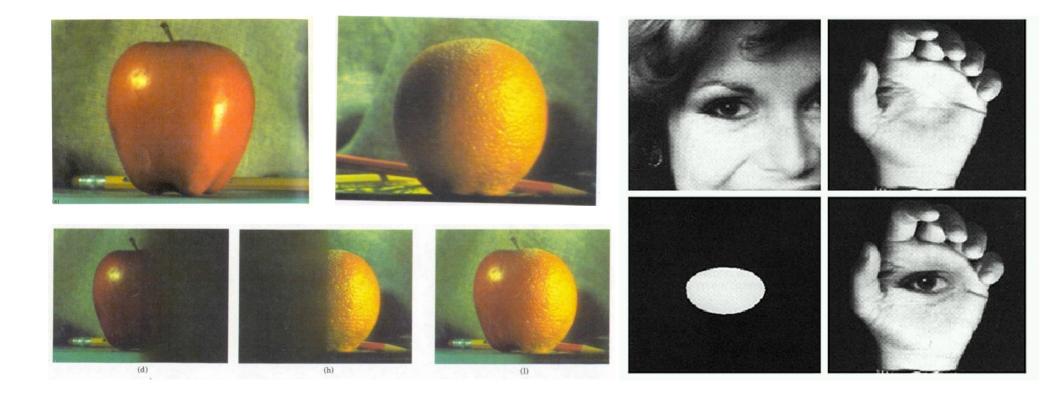








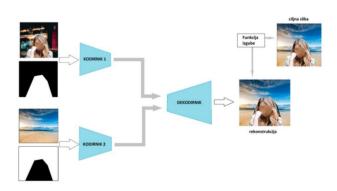
Merging examples





Compositing using imperfect masks

- Mask not following borders
 - User input
 - Low-resolution / speed
- Improve result using a deep model
 - Train using degraded masks as input
 - Compare to reference composite





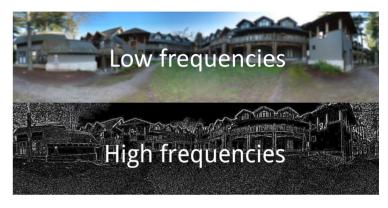
Examples

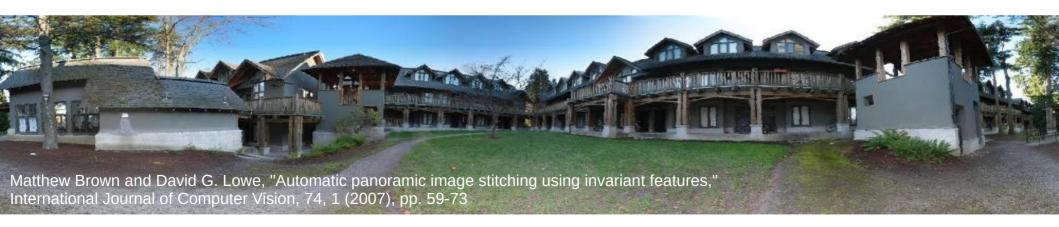




Merging examples - Autostitch

- Stitching panorama from multiple images
- Two-layer blending high and low frequencies
- Only blend low frequencies, keep high frequencies intact

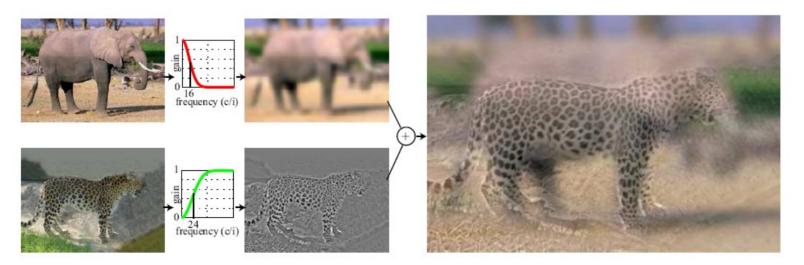






Hybrid images

- Static images with two interpretations
 - Low frequencies far away
 - High frequencies nearby





Hybrid images - examples







Interactive segmentation

- Determining segmentation mask is timeconsuming
 - Determine per-pixel assignment
 - Easy to make mistakes
- Content-aware interactive segmentation
 - Approximately state interest
 - Algorithm refines the mask on per-pixel level



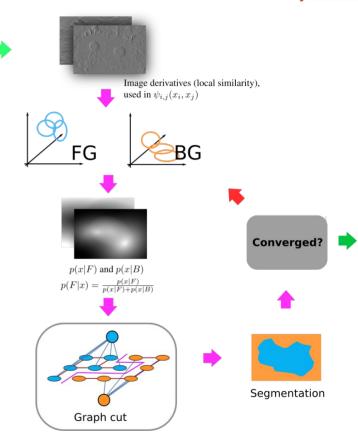
Segmentation with GrabCut

- Segmentation labels are highly structured
 - Two pixels that are similar are more likely in the same group
 - Two pixels that are near are more likely in the same group
- Formalized using Markov random field
- Solve MRF problem using Graph Cut



GrabCut algorithm

- Input: image, initial mask
- Compute local affinity for all pixels
- Iterate until convergence:
 - Estimate FG and BG models using mask
 - Compute model affinity for all pixels
 - Perform Graph cut for weights
 - Update mask with result



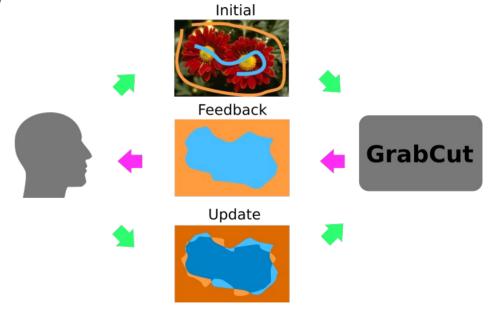
Image

Mask



Interactive segmentation

- User selects initial estimate of the object
 - Foreground, background, don't know
- Perform GrabCut with initial mask
- Present result to user
- User can correct result and restart with updated mask





Examples



Online demo (non-interactive): https://chocopoule.github.io/grabcutweb/ Interactive GrabCut: https://github.com/louisfb01/iterative-grabcut



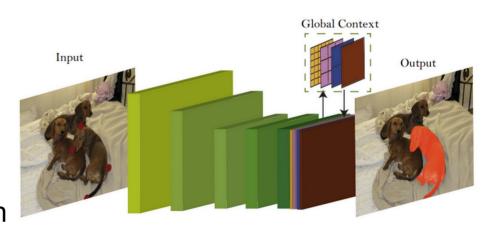
Segmentation with deep learning

- Train model to segment objects with limited data
 - Bounding box
 - Extreme points
 - Center + corners
- Use rich image structure to determine boundaries - segmentation



DEXTR architecture

- Input
 - Image
 - Extreme points encoded as gaussians
- Output binary segmentation
- Architecture DeepLab v2
- Training
 - COCO dataset
 - Simulate clicks from segmentation





DEXTR examples

