

1. Kateri od parov spodnjih izjavnih formul so enakovredni? Odgovor utemelji.

$$(a) \forall x (\exists y P(x, y) \wedge \exists y R(x, y)) \quad \text{in} \quad \forall x \exists y \exists z (P(x, y) \wedge R(x, z)),$$

$$(b) \neg \forall x \exists y (P(x) \wedge R(x, y)) \quad \text{in} \quad \forall y \exists x (\neg P(x) \vee \neg R(x, y)).$$

2. Dane so množice $A = \{1, 2, 3\}$, $B = \{2, 3, 4\}$ in $C = \{0, 1, 4, 5\}$. Določi spodnje množice (naštej njihove elemente).

$$(a) (B \setminus A) \cap C,$$

$$(b) C + (A \cup C),$$

$$(c) C + (A \cup B),$$

$$(d) A \cup (B \cap C),$$

$$(e) \mathcal{P}(A \cap B) \setminus C,$$

$$(f) \mathcal{P}(A \cap C) + \mathcal{P}(B \cap C),$$

$$(g) \mathcal{P}(A \cap C) + \mathcal{P}(A).$$

3. Določi množice:

$$(a) \emptyset \cap \{\emptyset\},$$

$$(b) \{\emptyset\} \cap \{\emptyset\},$$

$$(c) \{\emptyset, \{\emptyset\}\} \setminus \{\emptyset\}.$$

4. Ali veljajo naslednje enakosti oz. vsebovanosti z množicami? Dokaži ali pa poišči protiprimer.

$$(a) ((A \cap B) \cup (C \cap D))^c = (A^c \cup B^c) \cap (C^c \cup D^c),$$

$$(b) ((A \cup B) \cap (A \cup B^c)) \cup ((A^c \cup B) \cap (A^c \cup B^c)) = \mathcal{S},$$

$$(c) (A \cup B) \cap (A \cup B^c) \cap (A^c \cup B) \cap (A^c \cup B^c) = \emptyset,$$

$$(d) A \setminus (A \setminus (B \setminus (B \setminus C))) = A \cap B \cap C,$$

$$(e) A \setminus (B \cup C) = (A \setminus B) \cap (A \setminus C),$$

$$(f) A \cup (B + C) = (A \cup B) + (A \cup C),$$

$$(g) (A \cap B) \setminus C \subseteq (A \cup C) \cap B,$$

$$(h) (A + B) \setminus A = B \setminus A,$$

$$(i) (A + B) + (A + C) = A + (B + C),$$

$$(j) A + B \subseteq A + (B + C).$$